Auke Unibersity Edmund T. Pratt, Ir. School of Engineering

$\overset{ ext{Controls Fall 2016}}{ ext{Test II}}$

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Name and NetID (p	please print)	

In keeping with the Community Standard, I have neither provided nor received any assistance on this test. I understand if it is later determined that I gave or received assistance, I will be brought before the Undergraduate Conduct Board and, if found responsible for academic dishonesty or academic contempt, fail the class. I also understand that I am not allowed to speak to anyone except the instructor about any aspect of this test until the instructor announces it is allowed. I understand if it is later determined that I did speak to another person about the test before the instructor said it was allowed, I will be brought before the Undergraduate Conduct Board and, if found responsible for academic dishonesty or academic contempt, fail the class.

Signature:			

Instructions

First - please turn **off** any cell phones or other annoyance-producing devices. Vibrate mode is not enough - your device needs to be in a mode where it will make no sounds during the course of the test, including the vibrate buzz or those acknowledging receipt of a text or voicemail.

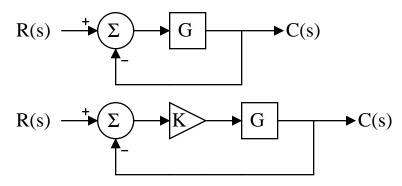
Please be sure to put each problem on its own page or pages - do *not* write answers to more than one problem on any piece of paper and do not use the back of a problem for work on a *different* problem. You will be turning in each of the problems independently. This cover page should be stapled to the front of Problem 1.

Make sure that your name and NetID are clearly written at the top of every page, just in case problem parts come loose in the shuffle. Make sure that the work you are submitting for an answer is clearly marked as such. Finally, when turning in the test, individually staple all the work for each problem and place each problem's work in the appropriate folder.

If you create some intermediate variable that is defined in terms of other known variables, you do not need to back-substitute later. For instance, if you have some $R_{eq} = R_1 + R_2$, from that point forward, you can use R_{eq} without having to expand it out.

Note that there may be people taking the test after you, so you are not allowed to talk about the test - even to people outside of this class - until I send along the OK. This includes talking about the specific problem types, how long it took you, how hard you thought it was - really anything. Please maintain the integrity of this test.

Note: The following represent the block diagrams for unity feedback systems and unity feedback systems with cascaded proportional (gain) control, respectively:



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Problem I: [24 pts.] Transient Characteristics

While your work for these problems may go on other pages, your final answers should go in the space provided below the prompts.

(1) Determine the steady-state value and the settling time of the step response for a system that has an overall transfer function of:

$$T_{\mathbf{w}}(s) = \frac{10}{s+4}$$

(2) Determine the steady-state value and the settling time of the step response for a unity feedback system that has a forward transfer function of:

$$G_{\mathbf{x}}(s) = \frac{15}{s+5}$$

(3) Determine the steady-state value, settling time, and %OS of the step response for a system that has an overall transfer function of:

$$T_{y}(s) = \frac{12}{s^2 + 4s + 20}$$

(4) Determine the steady-state value, settling time, and %OS of the step response for a unity feedback system that has a forward transfer function of:

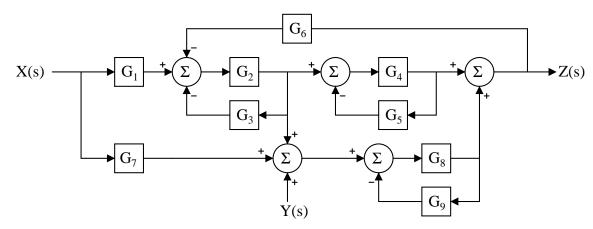
$$G_{z}(s) = \frac{25}{s^2 + 6s + 45}$$

- (5) A first-order system is found to have a step response with a steady state value of 11 and a settling time of 6 seconds. What is that system's overall transfer function?
- (6) An underdamped second-order system is found to have a step response with a steady state value of 0.25; the transient includes a maximum 50% overshoot that occurs 3 seconds after the step input begins. What is that system's overall transfer function?

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Problem II: [16 pts.] System Simplification

Given the system below:



- (1) Clearly draw a signal flow diagram for the system. Be sure to indicate where each node is on the diagram especially X, Y, and Z.
- (2) Clearly use Mason's Rule to determine the overall transfer function $T_x(s) = Z(s)/X(s)$. Note that once you define components in terms of the individual transfer functions, you do *not* need to simplify nor do you need to substitute them into the final result.
- (3) Clearly use Mason's Rule to determine the transfer function $T_y(s) = Z(s)/Y(s)$. Note that once you define components in terms of the individual transfer functions, you do *not* need to simplify nor do you need to substitute them into the final result. If you re-use any components defined for $T_x(s)$ above, simply state that.

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Problem III: [20 pts.] Stability and Steady State Analysis

While your work for these problems - including the Routh arrays - may go on other pages, your final answers should go in the space provided below the prompts. Clearly use a Routh array to support your conclusions for the following problems:

(1) A system has an overall transfer function of:

$$T_{\mathbf{w}}(s) = \frac{600(s+4)}{s^6 + 2s^5 - 7s^4 - 14s^3 - 144s^2 - 288s}$$

and Maple produces the following normalized Routh Table:

$$\begin{bmatrix} 1 & -7 & -144 & 0 & s^6 \\ 1 & -7 & -144 & 0 & s^5 \\ 5 & -21 & -144 & 0 & [s^4] \\ -7 & -288 & 0 & 0 & s^3 \\ -529 & -336 & 0 & 0 & s^2 \\ -1 & 0 & 0 & 0 & s \\ -1 & 0 & 0 & 0 & 1 \end{bmatrix}$$

How many left, right, and $j\omega$ poles does the overall system have?

(2) A unity feedback system has a (third order) forward transfer function of:

$$G_{\mathbf{x}}(s) = \frac{10}{s^3 + 10s + 15}$$

How many left, right, and $j\omega$ poles does the overall system have?

(3) Assume you have the system below with a plant G and an output transducer H of:

$$G(s) \xrightarrow{+} C(s)$$

$$G(s) = \frac{50}{(s+3)(s+4)}$$

$$H(s) = \frac{4a}{s+a}$$

- (a) Determine the conditions a for the system to be stable.
- (b) Are there one or more non-trivial values of a which would cause marginal stability? If so, find them and determine the frequency of oscillation when the system is marginally stable.
- (c) For values of a that keep the system stable, what is the system type from a steady-state error perspective?
- (d) Given that system type, determine the value for the appropriate finite (non-zero, non-infinite) static error constant and the steady state position error as a function of a.

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Problem IV: [20 pts.] System Analysis I

While your answers will generally not fit on this page, be sure to clearly indicate which part of the problem you are answering by writing the appropriate section/subsection/subsection before your answer. For example, "(6a): The settling time is..." A unity feedback system has a gain controller K in cascade with a plant:

$$G(s) = \frac{50}{(s)(s+4)(s+5)} = \frac{50}{s^3 + 9s^2 + 20s}$$

- (1) What system type does this represent?
- (2) Circle the appropriate statement or statements for each of the static error constants and line through the incorrect statements in the table below:

$K_{ m p}$	$K_{ m v}$	$K_{ m a}$
is 0	is 0	is 0
is ∞	is ∞	is ∞
is neither 0 nor ∞	is neither 0 nor ∞	is neither 0 nor ∞

- (3) For any of the above where you circled "is neither 0 nor ∞ " calculate the finite value of the static error constant as a function of K.
- (4) For any of the above where you circled "is neither 0 nor ∞ " find the gain K that would produce a position error of exactly 30%. Also determine the input signal for which that 30% error would represent an absolute position error of 4.
- (5) For the input signal you found in the previous problem, what is the smallest possible absolute position error you could achieve? What is the corresponding gain K to achieve that position error?
- (6) For a particular gain value, the poles of the overall transfer function are found to be:

$$s = -8.686, -0.157 \pm j4.153$$

- (a) Approximately what are the settling time and the %OS for the system with the gain required to produce those poles?
- (b) For the approximations above, how confident are you that they would stand up in comparison with values obtained through numerical simulation? Why do you say that?

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Problem V: [20 pts.] System Analysis II

While your answers will generally not fit on this page, be sure to clearly indicate which part of the problem you are answering by writing the appropriate section/subsection/subsection before your answer. For example, "(6a): For these poles, K=..." A system has an overall transfer function of:

$$T(s) = \frac{K(s+3)}{s^2 + 3s + Ks + 2 + 3K}$$

- (1) What system type does this represent?
- (2) Circle the appropriate statement or statements for each of the static error constants and line through the incorrect statements in the table below:

$K_{ m p}$	$K_{ m v}$	$K_{ m a}$
is 0	is 0	is 0
is ∞	is ∞	is ∞
is neither 0 nor ∞	is neither 0 nor ∞	is neither 0 nor ∞

- (3) For any of the above where you circled "is neither 0 nor ∞ " calculate the finite value of the static error constant as a function of K.
- (4) For any of the above where you circled "is neither 0 nor ∞ " find the gain K that would produce a position error of exactly 30%. Also determine the input signal for which that 30% error would represent an absolute position error of 4.
- (5) Determine the range of K that will produce an underdamped system.
- (6) For a particular gain value, the poles of the overall transfer function are found to be:

$$s = -2 \pm j$$

- (a) What is the gain value to get these system poles?
- (b) Approximately what are the settling time and the %OS for the system with this gain?
- (c) For the approximations above, how confident are you that they would stand up in comparison with values obtained through numerical simulation? Why do you say that?